

Track Reconstruction on GPUs for the Mu3e Experiment

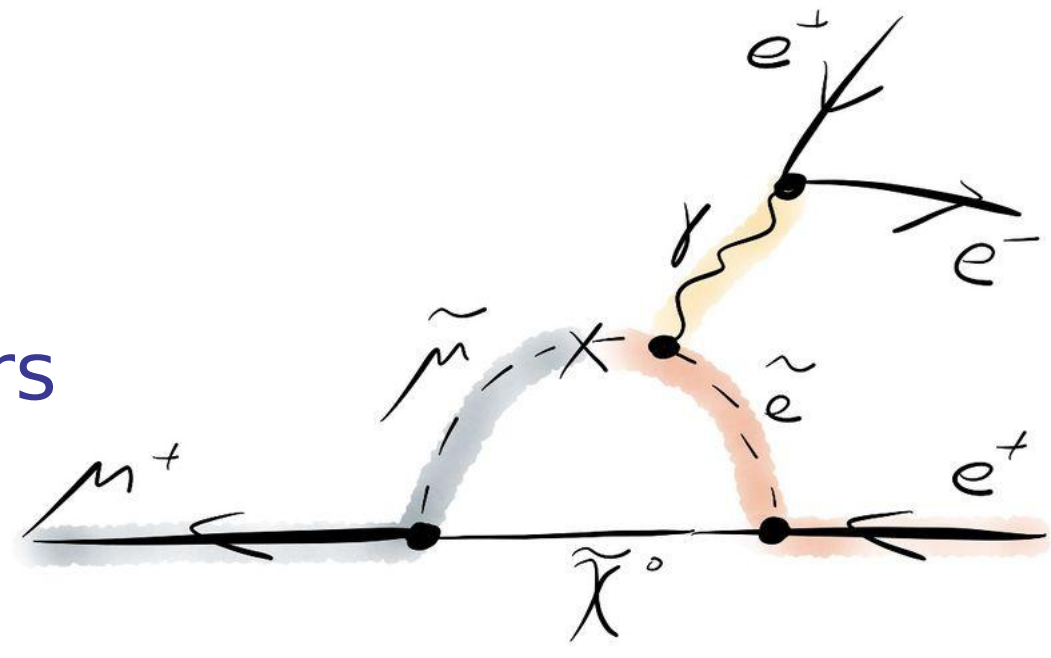
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Motivation

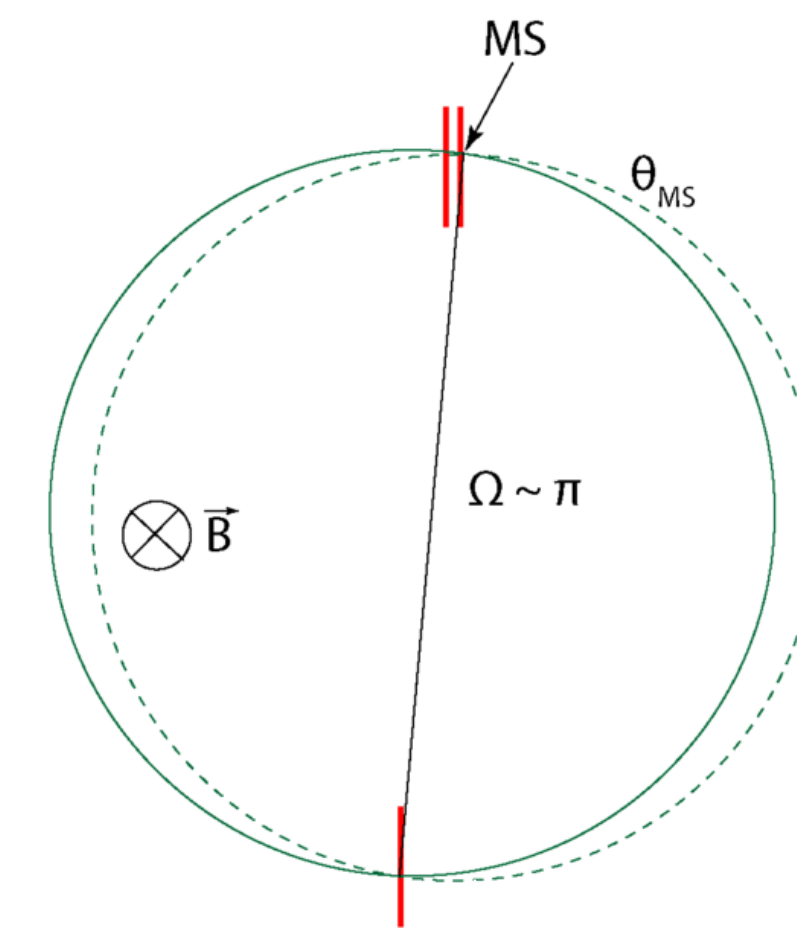
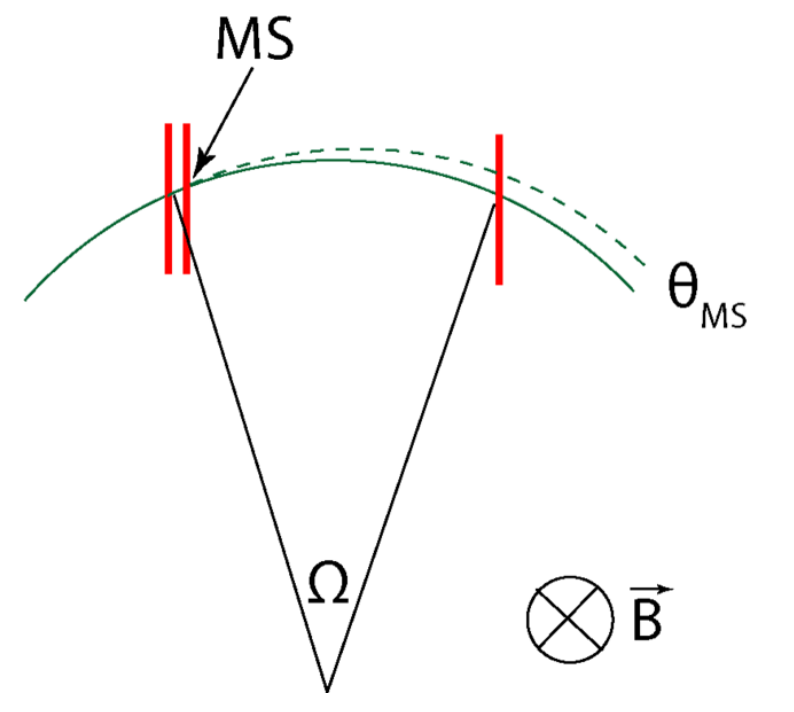
- ◆ Discovery of neutrino oscillations
→ Lepton flavour not conserved
- ◆ Lepton flavour violation in charged sector so far unobserved
- ◆ Mu3e searches for $\mu^+ \rightarrow e^+ e^+ e^-$
at a sensitivity of 1 in 10^{16} decays
- ◆ Requirements:
 - Rates $O(10^9 \mu/s)$
 - High precision tracking detectors
 - Excellent timing precision

⇒ Ultimately, improve sensitivity by 4 orders of magnitude compared to previous SINDRUM experiment ($BR < 10^{-12}$)



Momentum Resolution

- ◆ E_e : 10 - 50 MeV
- ◆ Momentum resolution dominated by multiple Coulomb scattering

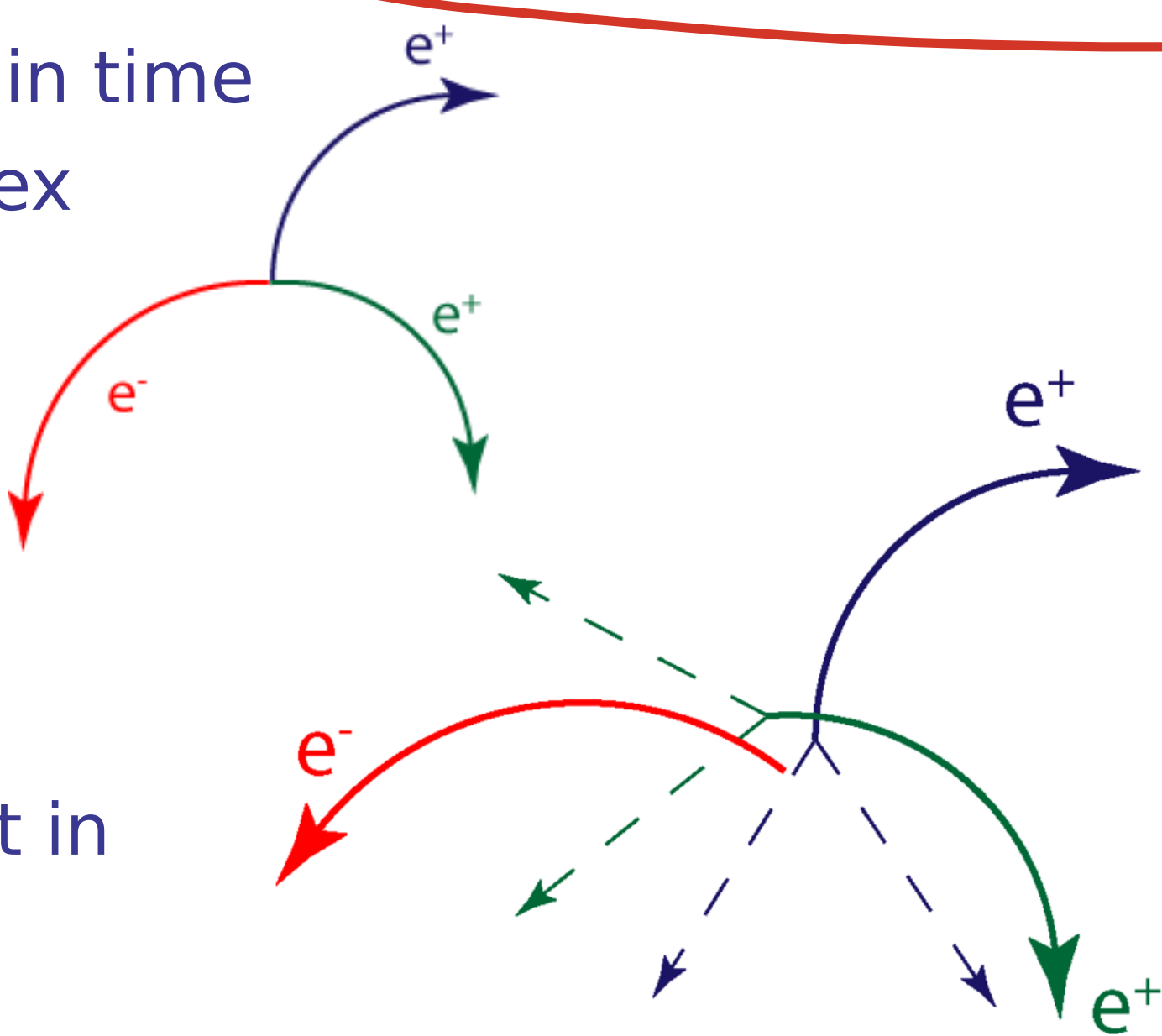


- ◆ Minimize material
- ◆ $\sigma_p/p \sim \theta_{MS}/\Omega$
- ◆ At $\Omega = \pi$, scattering cancels to first order
- ◆ Apply magnetic field
- ◆ Use recurring tracks

Signal & Background

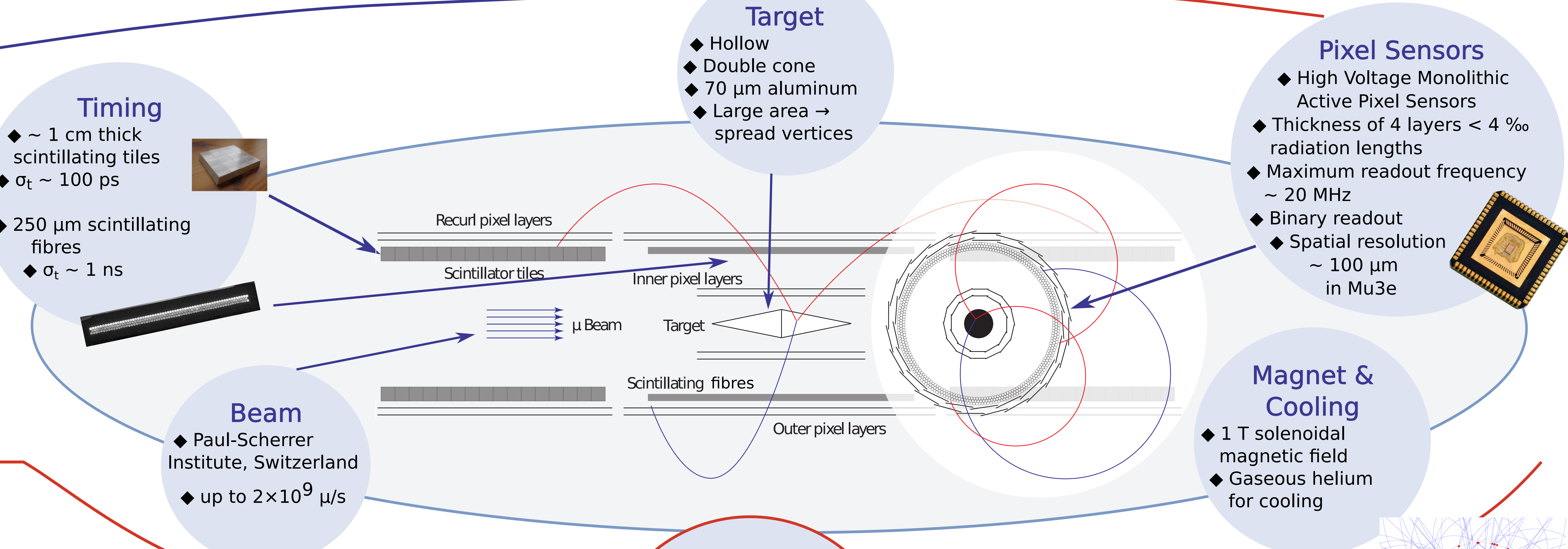
- ### Signal
- ◆ Coincident in time
 - ◆ Single vertex
 - ◆ $\sum \vec{p}_i = 0$

- ### Combinatorial Background
- ◆ Not coincident in time or place



- ### Beam
- ◆ Paul-Scherrer Institute, Switzerland
 - ◆ up to $2 \times 10^9 \mu/s$

- ### Timing
- ◆ ~ 1 cm thick scintillating tiles
 - ◆ $\sigma_t \sim 100$ ps
 - ◆ 250 μm scintillating fibres
 - ◆ $\sigma_t \sim 1$ ns



- ### Target
- ◆ Hollow
 - ◆ Double cone
 - ◆ 70 μm aluminum
 - ◆ Large area → spread vertices

- ### Pixel Sensors
- ◆ High Voltage Monolithic Active Pixel Sensors
 - ◆ Thickness of 4 layers < 4 % radiation lengths
 - ◆ Maximum readout frequency ~ 20 MHz
 - ◆ Binary readout
 - ◆ Spatial resolution ~ 100 μm in Mu3e

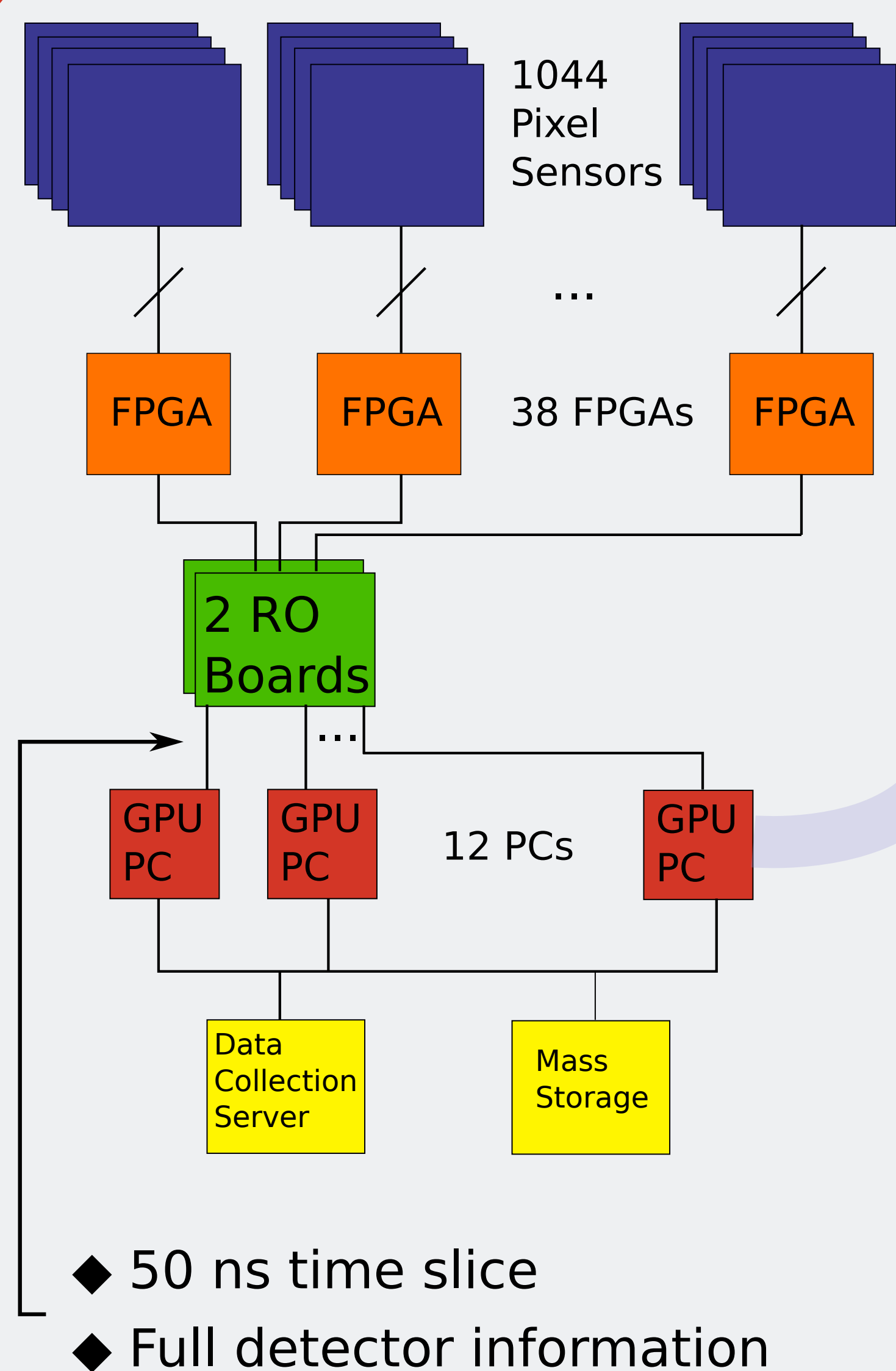
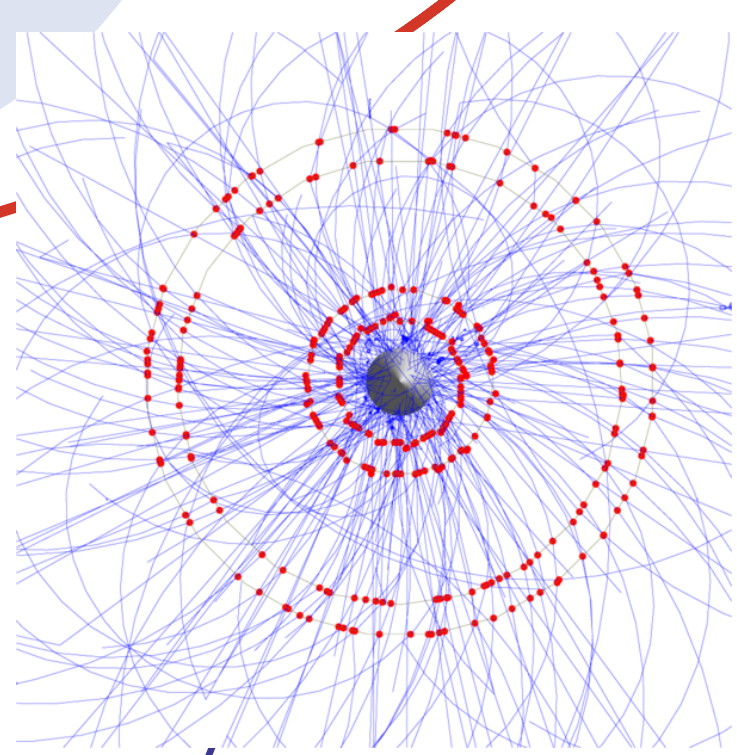
- ### Magnet & Cooling
- ◆ 1 T solenoidal magnetic field
 - ◆ Gaseous helium for cooling

- ### Readout
- ◆ Triggerless
 - ◆ ~ 1 Tbit/s to online farm
 - ◆ Track finding & reconstruction on GPUs

Reconstruction

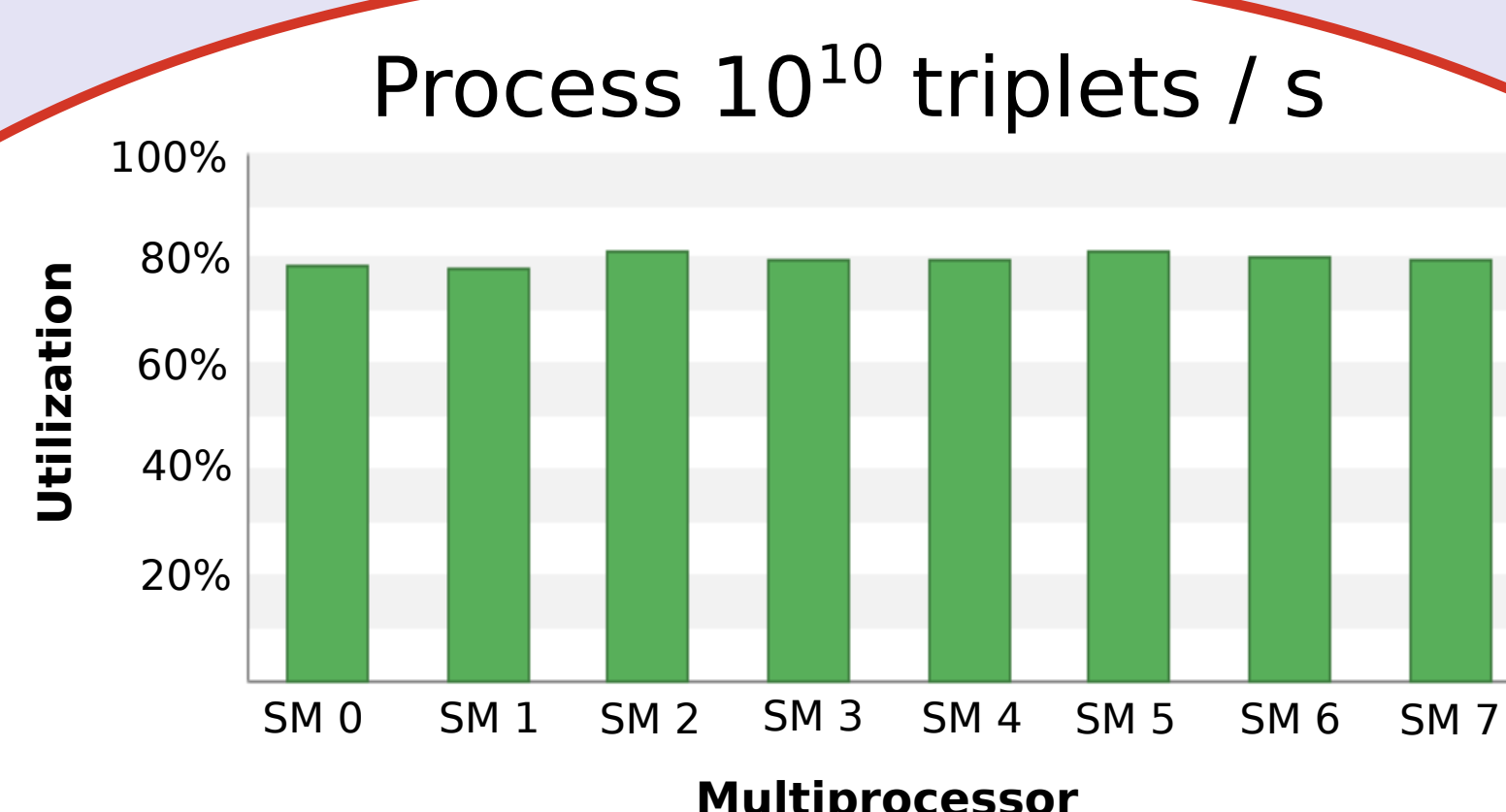
- ◆ Up to 100 tracks per readout frame of 50 ns (~ 1 Tbit/s)
- ◆ Reduce to ~ 100 Mbytes/s
- ◆ Triggerless → fully reconstruct on filter farm level

- ### Signal event:
- ◆ 3 tracks
 - ◆ Common vertex
 - ◆ No missing energy



- ◆ Ignore spatial uncertainty
- ◆ Describe track as sequence of hit triplets
- ◆ Multiple scattering at middle hit of triplet
- ◆ Minimize multiple scattering:

$$\chi^2 = \frac{\phi_{MS}^2}{\sigma_{MS}^2} + \frac{\theta_{MS}^2}{\sigma_{MS}^2}$$



Process 10^{10} triplets / s
Keeping 1536 cores busy
Using ~80 % of the GPU's compute capability

- ◆ Consider first three detector layers
- ◆ Number of possible track candidates ~ $n[1] \times n[2] \times n[3]$
- ◆ On GPU: Loop over all combinations
 - ◆ Geometrical selection cuts
 - ◆ Triplet Fit
 - ◆ Vertex Fit
- ◆ Compute in parallel on blocks and threads of GPU

~ 50 hits / plane / 50 ns
↓
100k combinations / 50 ns
↓
Filter farm with 50 GPUs

